

The (Mis)Allocation Channel of Climate Change

Evidence from Global Firm-level Microdata

Tianzi Liu Zebang Xu

Cornell University

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The Misallocation Channel of Climate Change

- Estimated macroeconomic consequences of climate change are significant:
 - Burke et al. (2015): $\approx 23\%$ of global GDP by 2100
 - Bilal et al. (2024): $> 50\%$ of global GDP by 2100
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Previous literature: climate change affects technology (\approx physical productivity)

- Heat drags down labor productivity, disrupts transportation...
- Temperature \uparrow \rightarrow production possibility frontier contracts \rightarrow Lower TFP
 - E.g. Machines are, on average, only 80% productive during heat shocks

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- In a distorted economy, there is dispersion in marginal products across firms:

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This paper: climate change affects **cross-firm misallocation**.

- Heat leads to inefficiencies: less productive firms ends up with too much capital
 - During heat shocks, the same machine will be more productive in a plant with ACs
- Temperature \uparrow → "investment mistakes" \uparrow → Lower TFP
- Climate change moves the economy further away from the efficient frontier

This paper...

Main Idea:

- Climate-induced misallocation is an **important driver** of aggregate climate damage

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The Plan:

1. Causal evidence and reduced-form measurement of climate-induced misallocation
2. Projection of global welfare losses under future climate change scenarios
3. Quantitatively understand the mechanisms in a firm dynamics model

Measurement: Climate-TFP Accounting

- A lower bound approach:
 - focusing on across-firm misallocation within each region-sector $n = (s, r)$.
- Similar to Hsieh and Klenow (2009), but all micro fundamentals can be affected by $\tilde{\mathbf{T}}_{rt}$.
- Total output is a CES aggregation of differentiated products,

$$Y_{nt} = \left(\int B_{ni}(\tilde{\mathbf{T}}_{rt}, \cdot)^{\frac{1}{\sigma_n}} Y_{nit}^{\frac{\sigma_n-1}{\sigma_n}} di \right)^{\frac{\sigma_n}{\sigma_n-1}},$$

- Subject to demand, firms face capital distortions in production:

$$\max_{P_{nit}, K_{nit}, L_{nit}} P_{nit} \underbrace{A_{ni}(\tilde{\mathbf{T}}_{rt}, \cdot) K_{nit}^{\alpha_{Kn}} L_{nit}^{\alpha_{Ln}}}_{Y_{nit}} - \left(1 + \tau_{ni}^K(\tilde{\mathbf{T}}_{rt}, \cdot)\right) R_{nt} K_{nit} - W_{nt} L_{nit}$$
$$\text{MRPK}_{nit} := R_{nt} (1 + \tau_{ni}^K(\tilde{\mathbf{T}}_{rt}, \cdot))$$

- Heterogeneity in $\tau_{ni}^K(\tilde{\mathbf{T}}_{rt}, \cdot)$ → Dispersion in MRPK across firms → Misallocation

Measurement: Climate-TFP Accounting

- Under the standard assumption of joint log-normality between A_{nit} , B_{nit} and $(1 + \tau_{nit}^K)$ in any cross-section, **aggregate TFP** of a region-sector $n = (s, r)$ can be decomposed as:

$$\log \text{TFP}_n(\check{\mathbf{T}}_{rt}, \cdot) = \text{Technology}(\check{\mathbf{T}}_{rt}, \cdot) - \underbrace{\frac{\alpha_{Kn} + \alpha_{Kn}^2(\sigma_n - 1)}{2} \text{var}_{mrpk_{ni}}(\check{\mathbf{T}}_{rt}, \cdot)}_{\text{MRPK Dispersion Across Firms}}$$

- Dispersion in MRPK lowers aggregate TFP.

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- Dispersion in MRPK lowers aggregate TFP.
- Why do climate shocks matter here? To fix ideas, consider the following:

Weather Forecast: Mild

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Realization: Mild

Realization: Heat wave

Year 1	Capital	MRPK
Ice Cream Parlor	5	2
Ski Resort	5	2

No Misallocation!

Year 2	Capital	MRPK
Ice Cream Parlor	5	3
Ski Resort	5	1

Large Misallocation!

The misallocation channel: how temperature affects misallocation

$$\frac{\partial \log TFP_n(\tilde{\mathbf{T}}_{rt}, \cdot)}{\partial \tilde{\mathbf{T}}_{rt}} = \frac{\partial \text{Technology}_{nt}(\tilde{\mathbf{T}}_{rt}, \cdot)}{\partial \tilde{\mathbf{T}}_{rt}} - \underbrace{\frac{\alpha_{Kn} + \alpha_{Kn}^2(\sigma_n - 1)}{2} \frac{\partial \text{var}_{mrpkni}(\tilde{\mathbf{T}}_{rt}, \cdot)}{\partial \tilde{\mathbf{T}}_{rt}}}_{\text{The Misallocation Channel}}$$

- Parameters can be directly calibrated: $\alpha_{Kn} = 0.35$, $\sigma_n = 4$.

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- Parameters can be directly calibrated: $\alpha_{Kn} = 0.35$, $\sigma_n = 4$.
- Firm-level microdata from 32 countries
 - Orbis Historic: 1995-2018 for 30 European countries
 - ▶ Good coverage of total sales in most countries
 - China NBS + India ASI
 - ▶ Census for “above-scale” manufacturing firms
 - Under Cobb-Douglas, we measure misallocation using

$$\text{var}_{mrpk_{nit}} = \text{var} \left[\log \left(\frac{\text{Revenue}_{nit}}{\text{Capital Stock}_{nit}} \right) \right]$$

for each region-sector-year.

- Weather and Climate Data: Daily Temperature from ERA5 $0.1^\circ \times 0.1^\circ$
- Medium-Range Weather Forecast Data (ECMWF)

Average Effect of Temperature on MRPK Dispersion

We regress MRPK dispersion on the distribution of daily temperatures.

$$\text{var}_{mrpk(s,r),t} = \sum_{b \in B/(5 \sim 10^\circ C)} \lambda_{\sigma_{mrpk}}^b \times \text{Tbin}_{r,t}^b + \delta_{\sigma_{mrpk}} \mathbf{X}_{s,r,t} + \theta_{c(r),s,t} + \eta_{s,r} + \varepsilon_{r,s,t}.$$

- r : region ("NUTS3"-level); s : sector (SIC industry group).
- $\mathbf{T}_{r,t} = \{\text{Tbin}_{r,t}^{<-5^\circ C}, \dots, \text{Tbin}_{r,t}^{>30^\circ C}\}$ as days in temperature bins.
- $\mathbf{X}_{s,r,t}$ is a vector of controls: number of firms, average sales and average MRPK.
- $\eta_{s,r}$: region-sector FE to remove "spurious" long-run relationship between $\mathbf{T}_{r,t}$ and development.
- $\theta_{c(r),s,t}$: country-sector-year FE to remove business cycles.
- SE clustered at the region level.

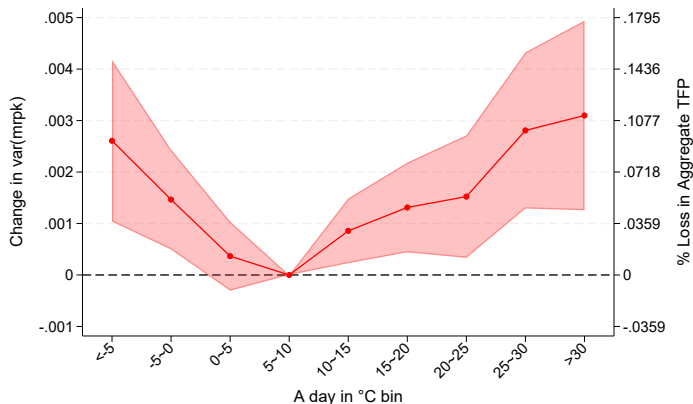
Within each region-sector, weather patterns are **exogenous** to capital distortions.

Average Effect of Temperature on MRPK Dispersion

$$\text{var}_{mrpk(s,r),t} = \sum_{b \in B / (5 \sim 10^\circ \text{C})} \lambda_{\sigma_{mrpk}^2}^b \times \text{Tbin}_{r,t}^b + \delta_{\sigma_{mrpk}^2} \mathbf{X}_{s,r,t} + \theta_{c(r),s,t} + \eta_{s,r} + \varepsilon_{r,s,t}.$$

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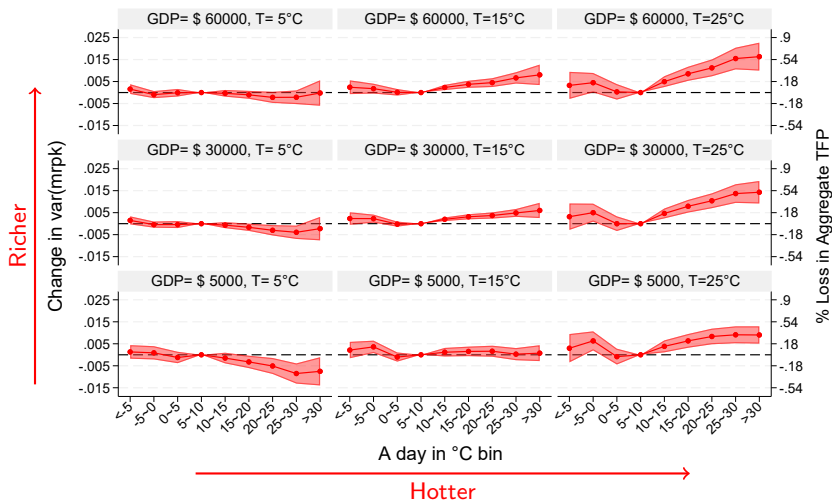
If we replace a 5-10°C (41°F to 50°F) day with a hotter-than-30°C (86°F) day in a year:

- The measured MRPK dispersion will increase by about 0.003;
- The measured yearly TFP will decrease by about 0.11% through capital misallocation.

→ $\approx \frac{1}{3}$ of daily GDP

Heterogeneous Effect across Regional Income and Long-run Climate

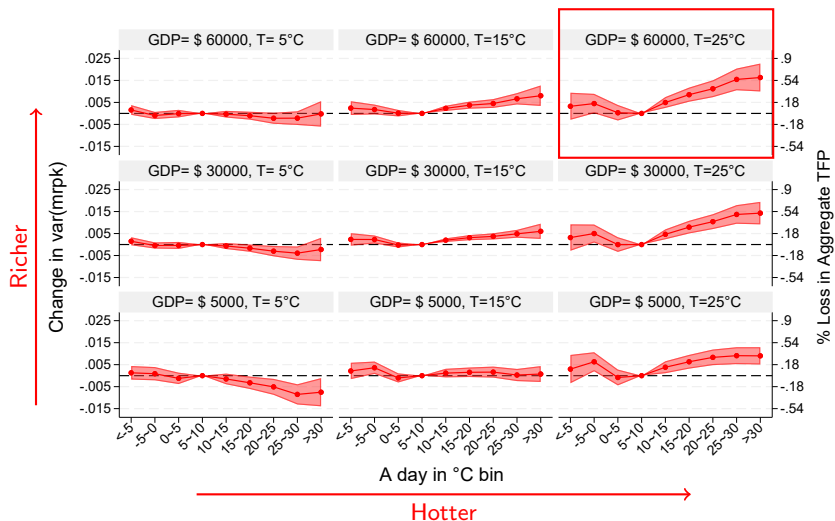
Heterogeneous Effect across Regional Income and Long-run Climate



In terms of the misallocation channel:

- Hotter and more developed regions are more susceptible to heat shocks.
- Cooler regions could even benefit from heat shocks.

Heterogeneous Effect across Regional Income and Long-run Climate



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End-of-the-century Projections under SSP3-7.0 Warming Scenario

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Under the assumption that $\frac{\partial \text{var}_{mrpk_{ni}}(\tilde{\mathbf{T}}_{rt, \cdot})}{\partial \tilde{\mathbf{T}}_{rt}} = f(\text{Long-run Climate, Income})$, we project the effect of climate-induced misallocation on aggregate TFP loss by the end of the 21st century (2081-2100) for 4,881 regions in 172 countries around the world.

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- The cost of climate-induced misallocation admits the following reduced-form decomposition:

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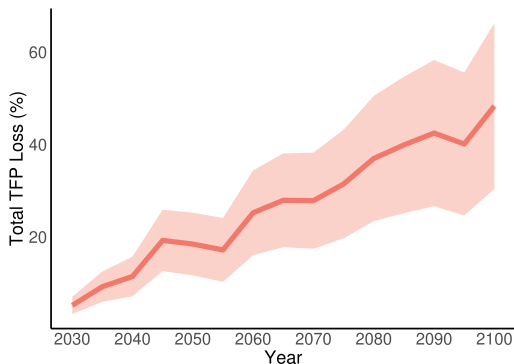
- The cost of climate-induced misallocation admits the following reduced-form decomposition:

$$\underbrace{\Delta^{\text{Loss}} \ln \text{TFP}}_{\text{Total Effect}=42.69\%} = \underbrace{\text{Weather Shock Effect}}_{4.99\%} + \underbrace{\text{Climatic Effect}}_{20.0\%} + \underbrace{\text{Income Effect}}_{17.7\%}$$

► Equation

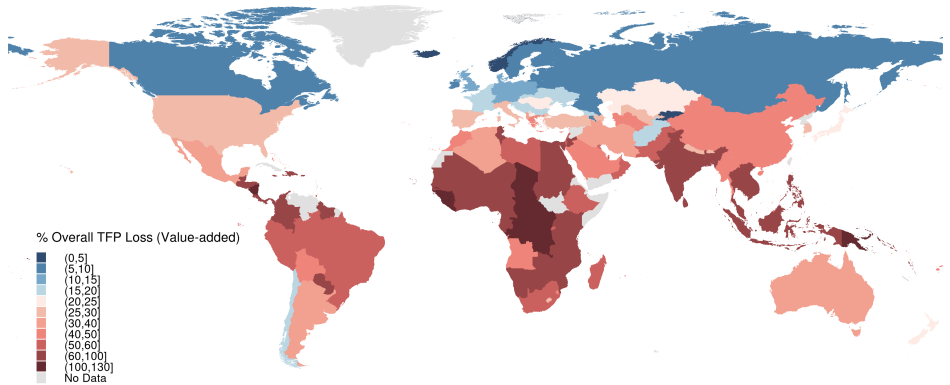
► Data

Figure: Global TFP Loss from the Misallocation Channel

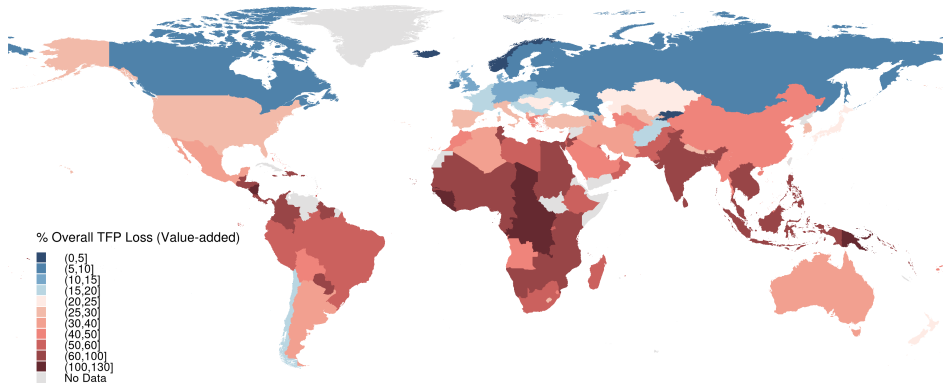


Future TFP Loss under SSP3-7.0 Warming Scenario

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Future TFP Loss under SSP3-7.0 Warming Scenario



→ Large spatial heterogeneity in projected damages from the misallocation channel:

- ▶ Above 60 %: Guinea, Congo, Malaysia, and India.
- ▶ 25-30 %: United States, Turkey, and Spain.
- ▶ Below 15 % : Norway, Finland, Canada, and Germany.

A Simple Model of Firm Dynamics

- We want to explain why both the levels and shocks of temperature matter for misallocation.
- A simple model with minimal ingredients: focusing on activities within (r, s) .
- Similar aggregation as the accounting framework: Iso-elastic demand + Cobb-Douglas Production
- Equilibrium revenue function: $P_{it} Y_{it} = \hat{A}_{it} K_{it}^{\alpha_K} N_{it}^{\alpha_N}$.

A Firm's productivity is heterogeneously impacted by temperature:

$$\hat{A}_{it} = \exp(\hat{\beta}_{it}(T_t - T^*)) \hat{Z}_{it}, \quad \hat{\beta}_{it} = \underbrace{\hat{\beta}_i}_{\text{Persistent sensitivity}} + \underbrace{\hat{\xi}_{it}}_{\text{Idiosyncratic sensitivity}}$$

← sensitivity deviation from optimal T^*

- Two sources of heterogeneity in $\hat{\beta}_{it}$:
 - $\hat{\beta}_i \sim \mathcal{N}(\overline{\hat{\beta}_i}, \sigma_{\hat{\beta}}^2)$ is known by the firm: e.g. products and adaptability.
 - $\hat{\xi}_{it} \sim \mathcal{N}(0, \sigma_{\hat{\xi}}^2)$ is i.i.d.: likelihood of extreme events scales with $(T_t - T^*)$.

MRPK and Temperature

- “Time-to-build” Capital \rightarrow Investment depends on expected productivity:

$$k_{it+1} \propto \mathbb{E}_t[a_{it+1}] \propto \hat{\beta}_i \mathbb{E}_t[(T_{t+1} - T^*)]$$

- After all shocks are realized, Relative MRPK is higher in the firms with higher unexpected changes in productivity:

$$\begin{aligned} mrpk_{it} - \overline{mrpk}_{it} &= \frac{1}{1 - \alpha_N} (\hat{a}_{nit} - \mathbb{E}_{t-1}[\hat{a}_{nit}]) \\ &= \frac{1}{1 - \alpha_N} \left\{ (\hat{\beta}_i - \overline{\hat{\beta}_i}) \underbrace{(T_{t+1} - \mathbb{E}_t[T_{t+1}])}_{T \text{ Forecast Error}} + \underbrace{\hat{\xi}_{it}(T_t - T^*)}_{\text{Damage Sensitivity Shock}} + \hat{\varepsilon}_{it} \right\} \end{aligned}$$

- Who gets lower $mrpk$ with a heat shock in a warm place? ($\eta_t > 0, T_t - T^* > 0$):
 - \rightarrow Heat-averse firms with $\hat{\beta}_i < \overline{\hat{\beta}_i}$: failed to expect the low productivity caused by the temperature shock η_t .
 - \rightarrow Unlucky firms with $\hat{\xi}_{it} > 0$: failed to expect the low productivity caused by the damage sensitivity shock $\hat{\xi}_{it}$.

Proposition: MRPK Dispersion The variance of $mrpk_{it}$ across all firms in a given period is:

$$\begin{aligned}\sigma_{mrpk,(r,s),t}^2 &= \left(\frac{1}{1 - \alpha_N} \right)^2 \text{Var}(\hat{a}_{nit} - \mathbb{E}_{t-1}[\hat{a}_{nit}]) \\ &= \left(\frac{1}{1 - \alpha_N} \right)^2 \left[\underbrace{(T_{r,t} - T^*)^2 \sigma_{\xi,(r,s)}^2}_{\text{Damage Volatility (Level Effect)}} + \underbrace{(T_{t+1} - \mathbb{E}_t[T_{t+1}])^2 \sigma_{\beta,(r,s)}^2}_{\text{Climate Volatility (Forecast Error Effect)}} + \sigma_{\varepsilon,(r,s)}^2 \right]\end{aligned}$$

- MRPK dispersion \propto TFP volatility \leftarrow endogenously generated by climate conditions.

How would climate change lead to larger misallocation?

- Larger deviation from optimal temperature: $(T_{r,t} - T^*)^2$
- Larger unexpected temperature shocks: $(T_{t+1} - \mathbb{E}_t[T_{t+1}])^2$

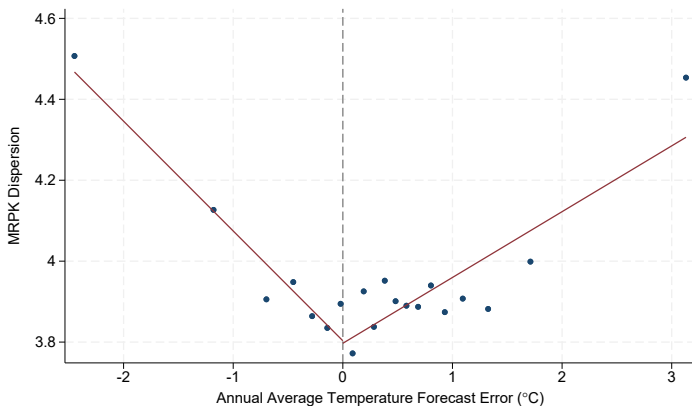
Forecast Error Effect: Climate Volatility

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- Mid-range temperature forecast data (1-month ahead forecast) from ECMWF.
- Misallocation is worse if the temperature forecast is overly cold or overly hot



Forecast Error Effect: Climate Volatility

$$\sigma_{mrpk,(s,r),t}^2 = \sum_{q \in \{\text{summer, winter, annual}\}} \theta_q \cdot \text{MSFE}_{q,r,t} + \gamma_1 T_{rt} + \gamma_2 T_{rt}^2 + \eta_{s,r} + \delta_{c(r),t} + \varepsilon_{s,r,t},$$

- $\text{MSFE}_{q,r,t}$: Mean Squared Forecast Error of monthly temperature.

$\text{MSFE}_{\text{annual},r,t}$	0.019114*** (0.006675)	0.016249** (0.006561)		
$\text{MSFE}_{\text{summer},r,t}$			0.014908** (0.007115)	0.016592** (0.007084)
$\text{MSFE}_{\text{winter},r,t}$			0.008536** (0.004017)	0.006096 (0.003882)
Quadratic Temperature Control	No	Yes	No	Yes
Region-Sector FE	Yes	Yes	Yes	Yes
Country-Year FE	Yes	Yes	Yes	Yes
Observations	124,065	124,065	124,065	124,065
R^2	0.876	0.876	0.876	0.876

- Forecast Errors are costly!

→ a 1°C error in temperature forecast for all months → **0.58 %** annual aggregate TFP loss

Level Effect: Temperature as volatility shock

$$\sigma_{mrpk,(r,s)t}^2 \propto \text{Var}(\hat{a}_{nit} - \mathbb{E}_{t-1}[\hat{a}_{nit}]) \propto \left[\underbrace{(T_{t+1} - \mathbb{E}_t[T_{t+1}])^2 \sigma_\beta^2}_{\text{Forecast Error Effect}} + \underbrace{(T_{r,t} - T^*)^2 \sigma_\xi^2}_{\text{Level Effect}} \right]$$

We proceed by testing whether firm-level TFP volatility varies non-linearly with the level of temperature in the sector-region panel:

$$\text{Var}_{(s,r),t}(\hat{a}_{it} - \hat{a}_{it-1}) = \alpha + \beta f(T_{r,t}) + \eta_{s,r} + \delta_{c(r),t} + \varepsilon_{s,r,t},$$

by using the “first-differenced” TFPR shocks.

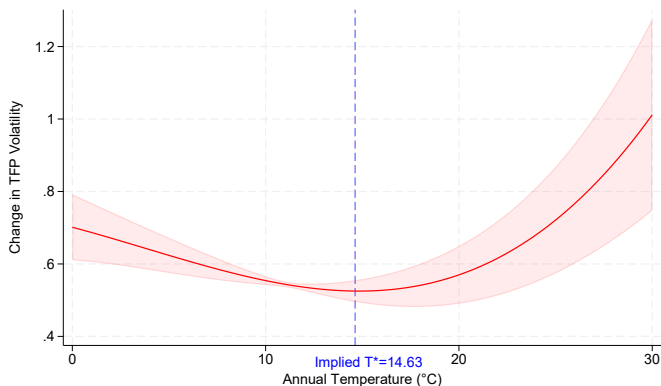
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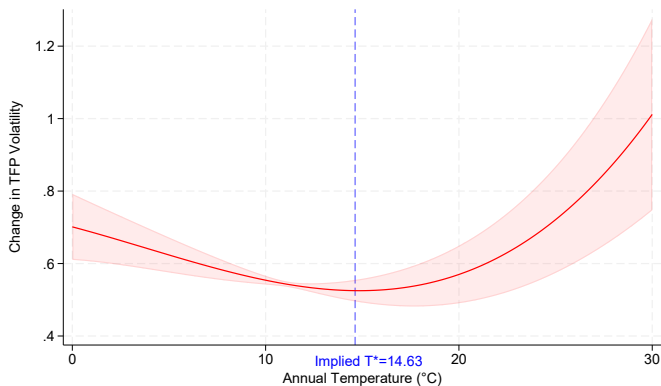
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- Firms' TFP volatility goes up in regions that are too hot or too cold.
- Optimal level of temperature is around 13 - 15°C ▶ Burke, Hsiang and Miguel 2015



Does climate matter? Yes!

Our model-implied regressions imply that:

- Climate-induced misallocation can explain 3.81% of TFP on average:

$$\begin{aligned}\Delta \log TFP_{(s,r),t} &= - \underbrace{\frac{\tilde{\alpha}_K + \tilde{\alpha}_K^2(\sigma - 1)}{2}}_{0.359} \Delta \sigma_{mrpk,(s,r),t}^2 \\ &= - \underbrace{\frac{\tilde{\alpha}_K + \tilde{\alpha}_K^2(\sigma - 1)}{2} \frac{\hat{\sigma}_{\xi,(s,r)}^2}{(1 - \alpha_N)^2} \overline{(T_{r,t} - T^*)^2}}_{\substack{\text{Level Effect} \\ =3.00\%}} \\ &\quad - \underbrace{\frac{\tilde{\alpha}_K + \tilde{\alpha}_K^2(\sigma - 1)}{2} \frac{\hat{\sigma}_{\beta,(s,r)}^2}{(1 - \alpha_N)^2} \overline{FE_{r,t}^2}}_{\substack{\text{Forecast Error Effect} \\ =0.81\%}} \\ &= 3.81\%\end{aligned}$$

- Volatility associated with temperature Levels account for 10% of the difference in aggregate TFP between India and EU.

Conclusions and Policy Implications

Conclusions and Policy Implications

- Established the first causal estimates and projections of the misallocation channel of climate change.
- Quantified the role of climate-induced volatility and weather forecasts in a firm dynamics model.
- Policies to manage climate-induced misallocation:
 - Mitigating global warming: $\approx 15\%$ TFP loss can be avoided under RCP 2.6 compared to RCP 7.
 - Improving mid-range temperature forecast accuracy
 - Reducing damage heterogeneity across units: “mind the laggards”!
 - ▶ More “equity” across firms → higher aggregate efficiency

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Preliminary Draft: zebangxu.com

tl567@cornell.edu zx88@cornell.edu

Identification of the Causal Elasticities

$$\text{var}_{mrpk(s,r),t} = \sum_{b \in B / (5 \sim 10^\circ C)} \lambda_{\sigma^2_{mrpk}}^b \times \text{Tbin}_{r,t}^b + \delta_{\sigma^2_{mrpk}} \mathbf{X}_{s,r,t} + \theta_{c(r),s,t} + \eta_{s,r} + \varepsilon_{r,s,t}.$$

- r : region ("NUTS3"-level); s : sector (SIC divisions).
- $\mathbf{T}_{r,t} = \{\text{Tbin}_{r,t}^{<-5^\circ C}, \dots, \text{Tbin}_{r,t}^{>30^\circ C}\}$ as days in each temperature bins.
- $\mathbf{X}_{s,r,t}$ is a vector of control: number of observed firms, average firm-level sales and average MRPK across firms.
- $\eta_{s,r}$: region-sector FE; $\theta_{c(r),s,t}$: country-sector-Year FE; SE clustered at region level..

Heterogeneous Regression Identification

- The same hot/cold day shock is likely to have heterogeneous across region-sectors.

▶ Het. effect across sectors

- Effect might be ambiguous:

- Heat-sensitive firms in hotter region might have greater incentives to adapt.
- But the marginal effect of hot temperatures in already hot locations might be worse.
- Firms in more developed regions find it easier to cope with weather damage
- But firm heterogeneity is larger in developed regions.

- Following the approach of Carleton et al. (2022), we interact the long-term annual average temperature of region r and average region-level annual GDP per capita with each temperature bin:

$$\begin{aligned} \sigma_{mrpk_{s,r,t}}^2 = & \sum_{b \in B/(5 \sim 10^\circ C)} \lambda_{\sigma_{mrpk}^2}^b \times Tbin_{r,t}^b + \sum_{b \in B/(5 \sim 10^\circ C)} \lambda_{\sigma_{mrpk}^2}^{b, \bar{T}} \times Tbin_{r,t}^b \times \bar{T}_r \\ & + \sum_{b \in B/(5 \sim 10^\circ C)} \lambda_{GDP_{pc}}^b \times Tbin_{r,t}^b \times \ln \overline{GDP}_{pc,r} + \delta_{\sigma_{mrpk}^2} \times \tilde{\mathbf{X}}_{s,r,t} + \alpha_{c,t} + \eta_{s,r} + \varepsilon_{s,r,t}, \end{aligned} \quad (1)$$

- Therefore, the first-order effect is region-specific:

$$\frac{\partial \text{var}_{mrpk_{s,r}}(\tilde{\mathbf{T}}_{rt, \cdot})}{\partial Tbin_{r,t}^b} \approx \lambda_{\sigma_{mrpk}^2}^b + \bar{T}_r \cdot \lambda_{\sigma_{mrpk}^2}^{\bar{T}} + \ln \overline{GDP}_{pc,r} \cdot \lambda_{GDP_{pc}}^b$$

End-of-the-century Projection of the Misallocation Channel

We project the effect of climate-induced misallocation on aggregate TFP loss by the end of the 21st century (2081-2100) for 4,881 regions in 172 countries around the world.

$$\underbrace{\Delta^{\text{Loss}} \ln \text{TFP}_r}_{\text{Total Effect}_r} = \frac{\alpha_{Kn} + \alpha_{Kn}^2(\sigma_n - 1)}{2} \left[\underbrace{\sum_b \left(\lambda^b + \lambda_{\text{GDP}_{pc}}^b \ln \text{GDP}_{pc,r,2019} + \lambda_{\bar{T}}^b \bar{T}_{r,2019} \right) \times \Delta \text{Tbin}_r^b}_{\text{Weather Shock Effect}_r} \right. \\
 \left. + \underbrace{\sum_b \lambda_{b,\bar{T}} \text{Tbin}_{r,\text{EOC}}^b \times \Delta T_r}_{\text{Climatic Effect}_r} \right. \\
 \left. + \underbrace{\sum_b \lambda_{\text{GDP}_{pc}}^b \text{Tbin}_{r,\text{EOC}}^b \times \Delta \ln \text{GDP}_{pc,r}}_{\text{Income Effect}_r} \right],$$

- Δ denotes changes between end-of-century (EOC) and 2019.

- *Weather Shock effect*: changes in daily temperature distributions
- *Climatic effect*: changes in elasticity due to shifts in long-run temperature
- *Income effect*: changes in elasticity due to economic development

Data Source for Projections

- Projection Data Source:

- Changes in daily temperature distributions and long-run temperature:

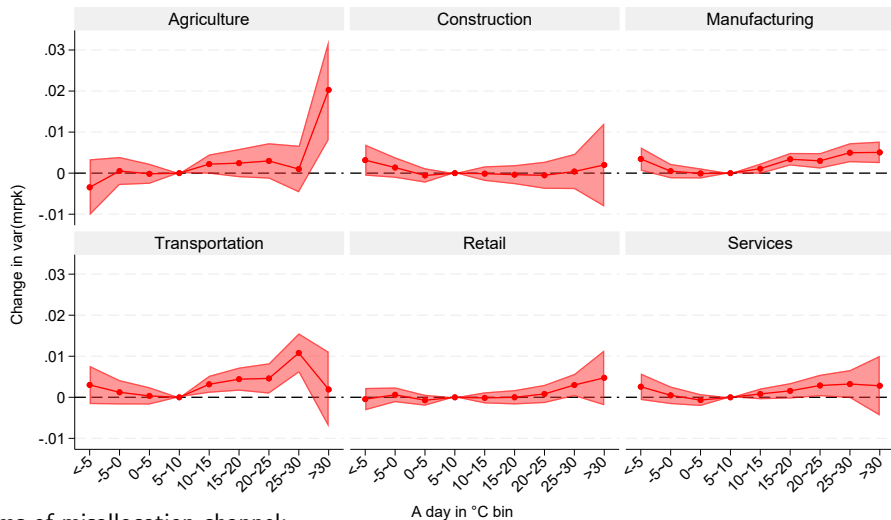
- ▶ Near-surface air temperature projection in SSP3-7.0 from CMIP-6 (ensemble average of 26 models).

- Changes in Income:

- ▶ OECD Env-Growth model (Dellink et al. 2017)
- ▶ Aggregation Weight: grid-level projected SSP-3 GDP (Wang and Sun 2022)

▶ Go Back

Heterogeneous Effect across Major Sectors

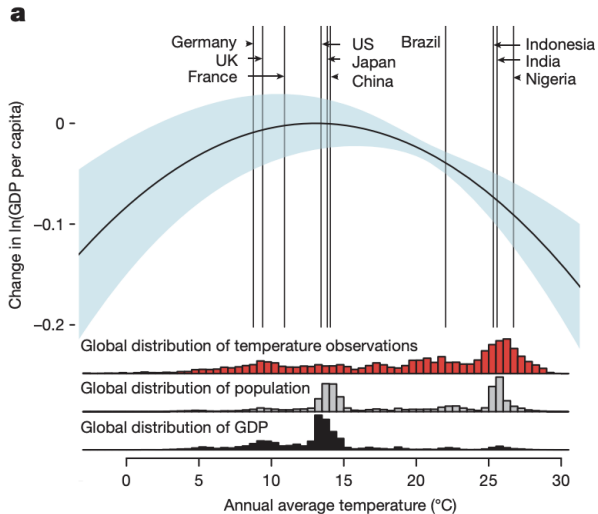


In terms of misallocation channel:

- The U-shaped pattern holds for all sectors.
- Agricultural and construction sector suffer the most. (a >30 °C day \approx 0.23% TFP loss)

Burke, Hsiang and Miguel 2015

Their finding: country-level economic production is smooth, non-linear, and concave in temperature with a maximum at 13°C.



Firm-level Evidence: Heterogeneity of β_i and MRPK Responses

$$mrpk_{it} - \overline{mrpk}_{it} = \frac{1}{1 - \alpha_N} \left\{ \underbrace{(\hat{\beta}_i - \overline{\hat{\beta}_i}) \eta_t^T}_{\text{Temp Shock}} + \underbrace{\hat{\xi}_{it}(T_t - T^*)}_{\text{Damage Sensitivity Shock}} + \hat{\varepsilon}_{it} \right\}$$

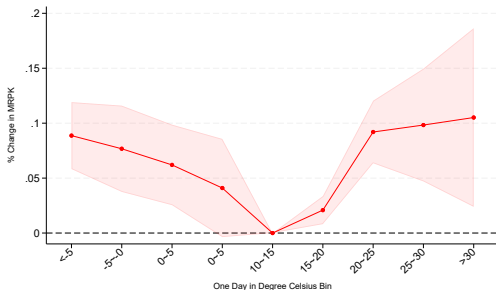
We run the empirical counterpart:

$$\begin{aligned} \log(MRPK_{r,s,i,t}) &= \sum_{b \in B / \{5-10^\circ C\}} \lambda_b \times \text{Tbin}_{r,t}^b \\ &+ \sum_{b \in B / \{5-10^\circ C\}} \lambda_{b, \hat{\beta}\text{-proxy}} \times \text{Tbin}_{r,t} \times \hat{\beta}\text{-proxy}_{it}^{r,s} + \delta \mathbf{X}_{i,t} \\ &+ \delta_i + \alpha_{s,c(r),t} + \varepsilon_{s,c(r),i,t}, \quad \hat{\beta}\text{-proxy} \in \{\text{Relative Size, AC}\}. \end{aligned} \quad (2)$$

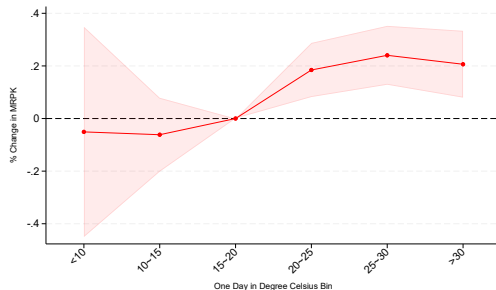
- Given it's hard to observe $\hat{\beta}_i$, we use two proxies:
 - Relative Size $_{it}^{r,s} := \log K_{it}^{s,r} - \overline{\log K_{it}^{s,r}}$ (Larger firms are more heat tolerant)
 - AC $_{it}^{r,s} = 1$ if ever reported an AC installation (a proxy for adaptability, only in India ASI)
- $\lambda_{b, \hat{\beta}\text{-proxy}}$ are identified by comparing firms within the same country-sector exposed to identical temperature shocks but show differential response in (log) MRPK.
 - A $\lambda_{b, \hat{\beta}\text{-proxy}} > 0$: relatively higher MRPK responses to shocks for heat-tolerant firms

Firm-level Evidence: Heterogeneity of β_i and MRPK Responses

(a) Heterogeneous Effect from Firm Size



(b) Heterogeneous Effect from Firm Adaptability (AC)

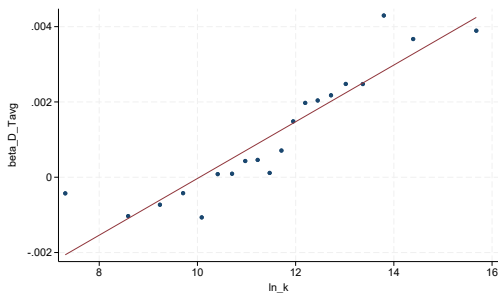


- An additional 30°C day relative to baseline:
 - makes a 1-SD larger firm having 0.1% higher MRPK compared to the average firm.
 - makes an AC-equipped firm having 0.2% higher MRPK compared to those without ACs.
- $\lambda_{b, \hat{\beta}\text{-proxy}} > 0$ for heat shocks

Firm-level Evidence: Heterogeneity of β_i and MRPK Responses

- This explains why richer regions suffer larger climate-induced misallocation \rightarrow larger heterogeneity in firm-level sensitivity!
- Across Firms within a region-sector: $\sigma_{\hat{\beta}}^2 \propto \sigma_k^2 \propto \text{GDP}_{pc}$

(a) $\hat{\beta}_i \propto k_{it}$



(b) Firm Size Dispersion and GDP per capita

